

Joint User-Centric Clustering and Pilot Allocation for Scalable Cell-Free Massive MIMO System

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Abstract. Cell-free massive multiple-input multiple-output (MIMO) is a promising technology where many access points (APs) cooperate to jointly serve user equipments (UEs) within the same time-frequency resource. However, the initial form of cell-free massive MIMO is not scalable when the number of UEs becomes very large. User clustering is a solution that can be used to make the system scalable as the number of UEs increases to infinity because each access point (AP) points progresses signals only from a subset of UEs it serves. The objective of this research is to design a joint user-centric clustering and pilot allocation system for scalable cell-free massive MIMO, which aims to achieve uniform spectral efficiency for all UEs. Therefore, this research aimed to combine the Gale-Shapley clustering algorithm with two existing pilot allocation methods, namely, the scalable and graph-coloring methods. The result showed that with 10 available orthogonal pilots, the scalable pilot allocation method achieves more than twice the 95%-likely spectral efficiency compared to the graph-coloring method. Furthermore, when the number of APs equals UEs, the complexity of the scalable method is linear in the number of UEs, as opposed to the polynomial complexity of the graph-coloring method.

Keywords: Beyond 5G; Cooperative communications; Linear beamforming; Network-centric; Uniform rate

1. Introduction

In cell-free massive multiple-input multiple-output (MIMO), all access points (APs) are cooperatively serving user equipments (UEs) in the network using the same time-frequency resources (Ngo *et al.*, 2017; Marzetta, 2015; Larsson *et al.*, 2014; Lu *et al.*, 2014). A central processing unit (CPU) communicates with APs through front haul links. In the downlink, data symbols were transmitted from the CPU to all APs, while in the uplink, APs sent soft estimated symbols or forwarded all received signals to the CPU. The method used is dependent on whether the processing was performed in a distributed or centralized fashion, respectively. However, this original cell-free massive MIMO is not scalable because the computational complexity becomes infinite when the number of UEs increases (Femenias, Riera-Palou, and Björnson, 2023; Papazafeiropoulos *et al.*, 2021; Bjornson and Sanguinetti, 2020; Interdonato, Frenger, and Larsson, 2019).

The user-centric cell-free massive MIMO introduced by Buzzi and D'Andrea (2017) is a practical method used to realize the benefits of coherent transmission. APs in the network

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MIMO context only served as a subset of UEs with the strongest channels (Xie *et al.*, 2023; Alonzo and Buzzi 2017; Gesbert *et al.*, 2010; Venkatesan, Lozano, and Valenzuela, 2007). It contrasts the network-centric method, where network densification generated more interference, especially for cell-edge UEs (Humadi *et al.*, 2022; Buzzi *et al.*, 2021). Consequently, the user-centric cell-free massive MIMO with distributed APs achieved better fairness and service uniformity among all UEs.

In cell-free massive MIMO, the number of UEs is typically much larger than the available orthogonal pilots, making it essential to associate UEs with APs and spectrum resources appropriately. The optimal joint design of APs selection and resource allocation included exhaustively searching all possible combinations of APs, UEs, and spectrum resources (Zeng *et al.*, 2021; Teng *et al.*, 2019; Liu and Lau, 2017). The optimal solution used to reduce the complexity and achieve scalable implementation, was to design a clustering algorithm, and then perform pilot allocation (Zhang, Yang, and Han, 2023; Ammar *et al.*, 2022; Zhong, Zhu, and Lim, 2022).

Recent research on scalable cell-free massive MIMO systems focused on clustering and pilot allocation frameworks. These frameworks are generally divided into graph-based methods (Huang et al., 2023; Liu et al., 2020b; Hmida et al., 2020) and non-graph based methods (Wang et. al., 2021; Liu et al., 2020a; Bjornson and Sanguinetti, 2020; Sabbagh, Pan, and Wang, 2018). For graph-based frameworks, an interference graph is generated after associating UEs with APs. The available orthogonal pilots are then assigned to each cluster with the aim of minimizing the number of possible pilots used and consecutively allocating different colors to overlapping clusters. Assuming the number of pilots available is at least equal to the chromatic number of the graph, the performance of such a method is guaranteed (Chartrand and Zhang, 2019). This is because severe performance degradation due to pilot contamination is avoided. Hmida et al. (2020) developed an edge when two UEs are dominant interferes to each other in order to reduce the impact of pilot contamination. However, Liu et al. (2020b) proposed reducing the subset of APs serving UEs when the available pilots are insufficient to satisfy the chromatic number of the graph. This method tends to reduce spectral efficiency performance since fewer APs serve UEs. To address this issue, Huang et al. (2023) proposed the clustering of users connected to the same APs using the K-means algorithm, before allocating pilots based on a weighted contamination graph for inter-cluster users.

A non-graph based framework (Sabbagh, Pan, and Wang, 2018) assigns dynamic pilot for pilot-sharing UEs that are sufficiently separated to meet the signal-to-noise ratio (SINR) constraint. Liu *et al.* (2020a) adopted a Tabu-search based pilot allocation method aimed to maximize the sum spectral efficiency. Meanwhile, Wang *et al.* (2021) studied APs-UEs association based on large-scale fading decoding coefficients, optimized using the max-min SINR criteria, although the specific method for pilot allocation was not stated. Bjornson and Sanguinetti (2020) proposed a joint clustering and pilot allocation strategy, where each UE selects one master AP with the best channel among the surrounding APs. Additionally, the master AP assigns the pilot with the least contamination among the available options.

All the previous research contributed to the realization of a scalable cell-free massive MIMO system. However, it is of interest to compare the performance of graph- and nongraph based pilot allocation schemes when using a common clustering algorithm. Lin *et al.* (2018) proposed a Gale-Shapley user-centric clustering algorithm designed explicitly for ultra-dense network (UDN). This algorithm used the stable marriage criterion (Alruwaili, Kim, and Oluoch, 2024; Teo, Sethuraman, and Tan, 2001) to determine the association between APs and UEs based on respective preference lists. The stable clustering ensured no APs and UEs left unpaired that would prefer each other over current partners. The proposed Gale-Shapley user-centric clustering algorithm (Lin *et al.*, 2018) offered a polynomial complexity for pairing APs-UEs, contrasting the exponential complexity of optimal exhaustive pairing. Moreover, Lin *et al.* (2018) proved the stability of APs and UEs association, indicating no blocking pairs existed. It was also reported that the proposed Gale-Shapley based clustering provided superior network performance in terms of the sum and UE rates. Despite several research on user-centric clustering for cell-free massive MIMO, not one had focused on the Gale-Shapley method (Huang *et al.*, 2023; Wang *et al.*, 2021; Bjornson and Sanguinetti, 2020; Hmida *et al.*, 2020; Liu *et al.*, 2020a; 2020b; Sabbagh, Pan, and Wang, 2018).

Based on the low complexity and superior performance of Gale-Shapley clustering, this research proposed a joint user-centric clustering and pilot allocation for scalable cell-free massive MIMO systems. The aim was to provide uniform spectral efficiency for all UEs in the network, which led to the following specific contributions.

- The Gale-Shapley clustering (Lin *et al.*, 2018) was combined with existing pilot allocation methods. This included the scalable (Bjornson and Sanguinetti, 2020) and graphcoloring methods (Liu *et al.*, 2020b). The Gale-Shapley clustering (Lin *et al.*, 2018) initially applied to UDN, considered the maximum number of UEs in APs as a constraint. In this research, the constraint is insignificant because the algorithm developed ensured that the number of serving UEs at each AP is equal to the available pilots.
- 2. Numerical analysis was conducted on the cumulative distribution function (CDF) of spectral efficiency per UE of both pilot allocation methods.
- 3. The complexity of both pilot allocation methods was compared to show the respective scalability performance.

2. System Model

Uplink communication is considered from K UEs to L APs equipped with N antennas, while only a single-antenna is used at UEs. The more practical time-division duplexing (TDD) mode selected, such that during τ_c channel coherence time, τ_u and τ_p channels were allocated for uplink data transmission and pilot training respectively. UEs and APs were uniformly distributed in a wrapped-around square area.

2.1. Channel Model

A quasi-static fading model was adopted (Aziz *et al.*, 2022) because the channel remained constant during each coherence block of duration τ_c and varied independently from one block to another. In each block, τ_p and τ_u channels were used for training and data transmission, respectively. The channel from UEs k to APs l was denoted as \mathbf{h}_{kl} and assumed to be a correlated Rayleigh fading channel $\mathbf{h}_{kl} \sim \mathcal{N}_C(0, \mathbf{R}_{kl})$, $\mathbf{h}_{kl} \in C^{Nx1}$. The matrix $\mathbf{R}_{kl} \in C^{NxN}$ described the spatial correlation among the channel elements in terms of large-scale fading power between UE k and AP l was analyzed by Bjornson and Sanguinetti (2020), and expressed in (equation 1).

$$\beta_{kl} = \frac{tr(\boldsymbol{R}_{kl})}{N} \tag{1}$$

where tr(.) is the trace of a matrix. The connectivity between the n^{th} antenna of serving AP l to UE k was defined by a diagonal matrix $A_{kl} \in C^{NxN}$. The n^{th} diagonal entry of A_{kl} is 1 when there is connectivity, and 0 if otherwise, allowing AP to transmit and decode the UE signal when connected. The matrix $C \in C^{KxL}$ represents the user-centric clusters, which are generally overlapping. When $C_{kl} = 1$, UE k is connected to at least one AP l antenna, also

translated as $tr(A_{kl}) > 1$, otherwise $C_{kl} = 0$. The subset of UEs connected to AP *l* was denoted as $\mathcal{A}_l = \{k: C_{kl} = 1, \forall k = 1, 2, ..., K\}$. Concatenating the connectivity matrix A_{kl} for all *L* APs diagonally formed a block-diagonal matrix $A_k \in C^{LNxLN}$. Clusters of two different UEs *k* and *j* overlap, $A_k A_j \neq \mathbf{0}_{LN}$, which means these were connected to the same APs, either partially or completely.

2.2. Pilot Training

Pilot training aimed to estimate the UEs channels at APs. In order to obtain a scalable system, APs were only required to estimate a subset of UEs channels, which were then used to combine the received signal (Bjornson and Sanguinetti, 2020). This process is known as the local partial minimum mean square (LP-MMSE) combiner.

The τ_p mutually orthogonal pilots were used for training purposes, where the number of UEs served by APs were assumed at most τ_p . This yielded τ_p –length pilot signals, where each was denoted as ϕ_{t_k} , $t_k = \{1, 2, ..., \tau_p\}$, satisfying $|\phi_{t_k}|^2 = \tau_p$. The limited number of pilots τ_p was due to spectrum availability. However, the number of UEs K was more significant than τ_p , and the pilots were reused among different UEs. The set \mathbb{Q}_k consisted of UEs, where each was allocated to pilot index t_k or ϕ_{t_k} . During training, AP*l* received the uplink pilot signal $\mathbf{r}_{t_k}^p$ from the UEs in set \mathbb{Q}_k , as provided in (equation 2).

$$\boldsymbol{r}_{t_k l}^p = \sum_{j \in \mathbb{Q}_k} \sqrt{\tau_p P_j} \boldsymbol{h}_{jl} + \boldsymbol{n}_l, \quad \boldsymbol{y}_{t_k l}^p \in C^{N \times 1}$$
(2)

The parameters τ_p and P_j define the processing gain and transmit power, respectively. Moreover, n_l is the additive white Gaussian noise (AWGN), distributed as $n_l \sim \mathcal{N}_C(0, \sigma^2 I)$.

Due to the limited availability of channels, the UEs in set \mathbb{Q}_k share the same pilots. This resulted in the received signal for UE k containing channels from other UEs $\mathbf{h}_{jl}, j \in \mathbb{Q}_k, j \neq k$. Therefore, the channel estimation of UEs in set \mathbb{Q}_k becomes correlated, leading to a phenomenon known as pilot contamination. The contaminated pilot degraded the performance of the channel estimator and consequently reduced the spectral efficiency. The MMSE channel estimate of \mathbf{h}_{kl} was expressed in (equation 3).

$$\widehat{\boldsymbol{h}}_{kl} = \sqrt{\tau_p P_j} \boldsymbol{R}_{kl} \boldsymbol{\psi}_{t_k l}^{-1} \boldsymbol{r}_{t_k l}^p$$
(3)

where $\boldsymbol{\psi}_{t_k l}$ is the correlation matrix of the received signal expressed in (equation 4).

$$\boldsymbol{\psi}_{t_k l} = \sum_{j \in \mathbb{Q}_k} \tau_p P_j \boldsymbol{R}_{jl} + \sigma^2 \boldsymbol{I} , \quad \boldsymbol{\psi}_{t_k l} \in C^{N \times N}$$
⁽⁴⁾

2.3. Data Transmission

During uplink data transmission, each AP received signals from all K UEs, as given in (equation 5).

$$\boldsymbol{r}_{l}^{d} = \sum_{j=1}^{K} \boldsymbol{h}_{jl} \boldsymbol{s}_{j} + \boldsymbol{n}_{l}$$
⁽⁵⁾

The parameter $s_j \in C$ represents the symbol of UEs *j* transmitted with power P_j . The uplink data can be decoded in two ways (Bjornson and Sanguinetti, 2020).

1) Centralized processing: APs send the received uplink signals during training and data transmission, i.e., r_l^p and r_l^d , respectively, to the CPU. This scheme requires significant bandwidth on the fronthaul link.

2) Distributed processing: APs independently send the local estimate of the data symbols to the CPU. Channel estimation was also performed locally in this scheme. It required significantly fewer bandwidth for fronthaul link and less CPU load.

This research focused on the distributed processing scheme. After channel estimation, APs applied the LP-MMSE combining vector, as provided in (equation 6).

$$\widehat{\boldsymbol{v}}_{kl}^{\text{LP-MMSE}} = P_k \left(\sum_{j \in \mathcal{A}_l} P_j \left(\widehat{\boldsymbol{h}}_{jl} \widehat{\boldsymbol{h}}_{jl}^{\text{H}} + \boldsymbol{C}_{jl} \right) + \sigma^2 \boldsymbol{I} \right)^{-1} \widehat{\boldsymbol{h}}_{kl}, \qquad \widehat{\boldsymbol{v}}_{kl}^{\text{LP-MMSE}} \in C^{Nx1}$$
(6)

APs are responsible for estimating the channel of the serving UEs, specifically those in \mathcal{A}_l . Moreover, the LP-MMSE combiner considered the source of interference for UE k that originated from the remaining UEs currently served by AP l, denoted by $j \in \mathcal{A}_l, j \neq k$. Therefore, this combiner is scalable and the complexity is unaffected by an infinitely large number of UEs. After receiving and combining the signals, APs locally computed the soft estimate of the data symbol of UEs k as defined in (equation 7).

$$\hat{s}_{kl} = \left(\hat{v}_{kl}^{\text{LP-MMSE}}\right)^{H} A_{kl} r_{l}^{d}$$
⁽⁷⁾

The soft-estimate was sent to the CPU for further processing, combining it with the estimated data symbol of UE k denoted as $\hat{s}_k = \sum_{l=1}^{L} \hat{s}_{kl}$. Due to the lack of channel estimation knowledge at the CPU, the use-and-then-forget (UatF) bound was used to calculate the achievable uplink spectral efficiency. This bound showed that the channel estimates were used to design the combining vector at APs, although it was discarded when calculating the achievable spectral efficiency at the CPU. The achievable spectral efficiency of UEs k can be determined as given in (equation 8).

$$SE_{k} = \frac{\tau_{u}}{\tau_{c}} \log_{2} \left(1 + \frac{P_{k} \left| E\{\left(\widehat{\boldsymbol{v}}_{k}^{\text{LP-MMSE}}\right)^{H} \boldsymbol{A}_{k} \boldsymbol{h}_{k}\}\right|^{2}}{\sum_{j=1}^{K} P_{j} \left| E\{\left(\widehat{\boldsymbol{v}}_{k}^{\text{LP-MMSE}}\right)^{H} \boldsymbol{A}_{k} \boldsymbol{h}_{j}\}\right|^{2} - P_{k} \left| E\left\{\left(\widehat{\boldsymbol{v}}_{k}^{\text{LP-MMSE}}\right)^{H} \boldsymbol{A}_{k} \boldsymbol{h}_{k}\right\}\right|^{2} + \sigma^{2} E\{\|\boldsymbol{A}_{k} \boldsymbol{v}_{k}\|\}^{2}\right)$$
(8)

The combining vector $\hat{v}_{k}^{\text{LP-MMSE}} \in C^{NL \times 1}$ was derived from stacking $\hat{v}_{kl}^{\text{LP-MMSE}}$, $\forall l = 1, 2, ... L$. Similarly, $h_k \in C^{NL \times 1}$ was obtained from stacking $h_{kl} \forall l = 1, 2, ... L$, whereas $A_k \in C^{NL \times NL}$ is defined as $I_L \otimes A_k$, where \otimes is Kronecker product and I_L is identity matrix of size L.

3. Joint User-Centric Clustering and Pilot Assignment

A strategic method to associate UEs with APs and allocated pilots effectively is required since the number of UEs is typically larger than the number of available orthogonal pilots. A joint user-centric clustering and pilot allocation method designed for a scalable cell-free massive MIMO system was proposed to address this challenge.

3.1. Proposed Method

The Gale-Shapley clustering (Lin *et al.*, 2018) was combined with existing pilot allocation methods, namely the scalable (Bjornson and Sanguinetti, 2020) and graph-coloring methods (Liu *et al.*, 2020b). This algorithm which was previously applied to UDN, considered the maximum traffic-load at APs as constraint. However, the constraint was omitted and instead equivalently limited the number of serving UEs at each AP by the available orthogonal pilots τ_p .

According to Lin *et al.* (2018), clustering comprised of two stages, namely anchoring and exploration. Initially, UEs measured the large-scale fading β_{kl} from the received synchronization signal and generated the preference list based on these measurements. APs produced the preference list using the same steps. To determine the anchor AP, UE proposed the most preferred AP which had not been rejected initially and is waiting for acceptance or rejection. Meanwhile, each AP retained all UE proposals until the limit τ_p was reached, after which it kept only τ_p best channel UEs and rejected the rest. The rejected UEs then proposed to the following preferred AP, and the process is repeated until the proposal of a given UE is either accepted or all proposals are rejected by all APs in the preference list of the UE.

The exploration stage was conducted only for APs with fewer associated UEs less than τ_p . This is different from the method proposed by Lin *et al.* (2018), where the maximum traffic- load at APs was considered. To ensure UEs with acceptable channel conditions, a threshold γ was defined. It is essential to set γ to a low enough value such that more UEs will be served by APs. For UEs with $\beta_{kl} \geq \gamma$, AP *l* firstly sorts them and then associates with the top β_{kl} list, as long as the total number of UEs, including those from the anchoring stage, does not exceed τ_p . At the end of the exploration stage, each UE can be associated with more than 1 APs leading to many-to-many matching. In addition, the subset of APs serving a given UE may partially overlap.

Two pilot allocation methods, namely scalable, non-graph based, and graph methods, were examined.

3.1.1. Scalable Method

The scalable pilot assignment method (Bjornson and Sanguinetti, 2020) was applied to the constructed clusters. Firstly, the joint clustering and pilot assignment, in the original form, were briefly introduced. In the process, UEs selected master AP that had the best channel among its surrounding APs. Subsequently, the master AP assigned the least pilot contamination among the τ_p available option. The surrounding APs determined whether to jointly serve the new UE based on the absence of currently served UEs using the same pilot or if the interference level of the allocated pilot signal is not significantly larger than that measured from its master AP.

The scalable method does not guarantee that UEs served by a given AP have orthogonal pilots as opposed to the Gale-Shapley exploration stage, which rejected UEs based on the large-scale fading coefficient β_{kl} . This led to two potential outcomes. Firstly, there may be more τ_p UEs designating the same master AP, causing it to allocate pilots with the least corresponding interference level. Secondly, the surrounding APs serve the new UE, which has the same pilot already allocated to its currently served UE.

The research focused solely on the anchoring stage of the Gale-Shapley algorithm with anchor AP as the master (Bjornson and Sanguinetti, 2020). Moreover, it only accepted proposals from at most τ_p best channel UEs. The process guaranteed orthogonal pilots were assigned to the associated UEs, as opposed to the original version (Bjornson and Sanguinetti, 2020). Similar to the original version, after finding an anchor AP, the surrounding APs jointly served the new UE when they have no UEs served using the same pilot as the new UE or when the interference level of the allocated pilot signal was not significantly larger than that measured from its master AP.

3.1.2. Graph-coloring Method

After defining the user-centric clusters, the next step entailed pilot allocation to each cluster. In the context of graph-coloring, each UE is defined as a vertex. Furthermore, two UEs with overlapping clusters were connected by an edge, indicating that at least common APs served the purpose. The connected vertices known as adjacent vertices were assigned

orthogonal pilots to prevent the adverse impact of pilot contamination on the system performance. However, due to the limited number of available pilots, designing an effective allocation scheme challenges. The graph-coloring method (Liu *et al.*, 2020b) was used to allocate the limited number of orthogonal pilots to the user-centric clusters.

Graph-coloring aims to minimize the number of colors applied to the vertices, ensuring that that adjacent ones have different colors (Chartrand and Zhang, 2019; Formanowicz and Tanas, 2012; Cheng *et al.*, 2005). Initially, the algorithm calculates the degree of each vertex, which is defined as the number of connected edges. The vertex with the highest degree is colored first. Subsequently, the saturation degree of adjacent vertices was updated, indicating the number of unique colors assigned. The next vertex to be colored was selected based on the one with the maximum saturation degree. These steps were repeated until all vertices were colored. However, when the total number of colors is not equal to τ_p , the clustering exploration stage must be repeated. During this stage, the threshold γ is either increased or decreased, depending on whether the number of colors is higher or lower than the available τ_p colors, respectively.



Figure 1 CDF of spectral efficiency per UE for increasing number of UEs; number of pilots available $\tau_p = 5$, number of APs L = 100

3.2. Complexity Comparison

The complexity comparison was performed between the two pilot allocation methods. Based on calculation provided in (Chen *et al.*, 2021), the scalable pilot allocation method has a complexity order of O(L + K), while the graph-coloring pilot assignment is of order $O(K^2 + KL + KL\log_2(L))$. This suggested that the scalable pilot allocation method offered better scalability as $K \to \infty$.

4. Results and Discussion

The system performance was evaluated in terms of the CDF of spectral efficiency per UE for an increasing number of UEs and available pilots. However, since the main aim of cell-free massive MIMO is to provide uniform service for all UEs in the network, this research focused on the 95%-likely spectral efficiency to measure the performance of the lowest 5% UE accurately. The number of UEs considered were K = 50, 100, and 200, while the available orthogonal pilots were $\tau_p = 5$ and 10. There were L = 100 APs, where each was equipped with N = 4 antennas. Furthermore, the single-antenna UE has a transmission power of $P_k = 100$ mW. A large-scale fading channel model similar to the one designed by Bjornson, Hoydis, and Sanguinetti (2017) was adopted. The channel coherence time was set at 200 blocks, allocating $200 - \tau_p$ blocks for data transmission. During the exploration

stage, a default threshold γ value of -40 dB was used. Both UEs and APs were uniformly distributed in a 500-meter-square wrapped-around area.

Figure 1 shows the CDF of spectral efficiency per UE when each AP serves at most $\tau_p = 5$ UEs. As the number of UEs increases, both the graph and scalable pilot allocation schemes experience decline in because more UEs translate to higher inter-cluster interference in the network. This is a consequence of the low complexity combining vector, which mainly suppresses the interference signals from UEs served by the given APs, as stated in Eq. (6). The performance of the graph pilot allocation method is worse than the scalable at lower spectral efficiency values, and vice versa. The limitation of $\tau_p = 5$ pilots per AP in the scalable method leads to severe pilot contamination when the master AP serves more than 5 UEs, resulting in reduced spectral efficiency, particularly evident in the upper part of Figure 1. However, the graph-coloring only allocated orthogonal pilots when common APs serve two different UEs. To fulfill the restricted number of pilots, the graph method reduces the number of cooperating APs for a given UE. This leads to less spatial diversity, which impacts the UEs with low to moderate channel conditions, resulting in lower spectral efficiencies compared to the scalable method.



Figure 2 CDF of spectral efficiency per UE for increasing number of UEs; number of pilots available $\tau_p = 10$, number of APs L = 100

The CDF of spectral efficiency per UE was compared as the number of orthogonal pilots increased from $\tau_p = 5$ to 10, shown in Figure 2. Similar to the scenario of having $\tau_p = 5$ pilots per AP, as the number of UEs is increased, the UE rate decreases. Additionally, both the graph and scalable methods had similar performance when there were more pilots in the system. This is because a greater number of orthogonal pilots reduced the impact of pilot contamination for the scalable method, leading to a uniform increase in UEs spectral efficiency for all UEs. However, increasing the number of pilots for the graph method significantly benefited UEs with low spectral efficiency. This was proven by the lower part of the spectral efficiency curve in Figure 1, which rose as the number of pilots increased in Figure 2. The reverse was the case in the upper part of the curve because each AP served more UEs when the number of pilots was increased. However, the UEs that initially had high spectral efficiency were sacrificed due to increased inter-cluster interference. As a result, increasing the number of pilots provided uniformly superior performance for both pilot allocation methods.

The 95%-likely spectral efficiency for all scenarios showed that the scalable method is superior compared to the graph method. For example, in Figure 1, when K = 50, $\tau_p = 5$, the scalable and graph methods obtained a 95%-likely spectral efficiency of 1.370 and 0.673, respectively. Increasing the number of UEs to K = 200 while ensuring the number of pilots

fixed, the 95%-likely spectral efficiency reduces to 0.063 and 0.050 for the scalable and graph methods, respectively.

When the number of UEs in the network is low, such as 50, the APs are associated with distant UEs. Due to the insufficient number of pilots, the subset of serving APs was reduced since the graph method needed to assign different colors to adjacent vertices. Therefore, the spectral efficiency per UE of the graph method is much lower. The scalable method tends to allocate the same pilot to overlapping clusters. When the number of UEs is fewer, the average distance is high, causing the impact of inter-cluster interference to be compensated with the benefit of associating each UE with more serving APs.

Increasing the number of available pilots to $\tau_p = 10$ increases the 95%-likely spectral efficiency across all UEs scenario for both methods, as shown in Figure 2. For example, when K = 50, the scalable and graph methods produced 95%-likely spectral efficiencies of 1.922 and 1.682, respectively. In contrast, the corresponding spectral efficiencies were 0.202 and 0.093 when K = 200. The increased availability of pilots reduced the impact of pilot contamination, leading to enhanced spectral efficiency. The graph method produced more APs serving a given, significantly improving the performance. Despite this fact, the scalable method remains more attractive, since it provides a uniformly superior performance with lower complexity.

5. Conclusions

In conclusion, a joint user-centric clustering and pilot allocation method was for scalable cell-free massive MIMO systems aimed at providing uniform spectral efficiency for all UEs in the network. The performance of the graph pilot allocation method was particularly sensitive to the insufficiency of orthogonal pilots, as it relied on following the chromatic number of the graph. UEs were served by a lesser number of APs, which deteriorated the respective spectral efficiencies. Despite the uniformly superior performance, the scalable pilot allocation method had lower complexity, making it a feasible choice for realizing a scalable cell-free massive MIMO system, especially in scenarios with higher UE density. The analysis provided uniform power transmitted from all UEs with interest in optimization despite the higher complexity and signalling overhead required. UEs were assumed static throughout the research, therefore, evaluating the impact of UEs mobility on the system performance was suggested for future investigations.

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